# GOA BOARD OF SECONDARY AND HIGHER SECONDARY EDUCATION SECOND TERM EXAMINATION <br> MODEL PAPER ( 2022 - 2023 ) 

STD : X
MAX MARKS : 40
SUBJECT : MATHEMATICS (E) - LEVEL 2
TIME : 1hr 45 minutes

INSTRUCTIONS : i) Answer each main question on a fresh page.
ii) All questions are compulsory.
iii) The question paper consists of four questions, each of 10 marks
iv) There is no overall choice.
v) In questions on constructions, the drawing should be clear and exactly as per the given measurements. The construction lines and arcs should be maintained.
vi) Use of calculators and mathematical tables is not permitted.

Q1A) Find the class size of the class intervals $25-55,55-85,85-115, \ldots$
B) Attempt the following :
(i) Write the first four terms of an AP having first term as 19 and common difference as -3 .
(ii) State with reason if the given list of numbers is an AP or not. $1,3,9,27, \ldots$
C) Answer the following questions with reference to the given Arithmetic Progression : 11, 15, 19, 23,...
(i) Find the $20^{\text {th }}$ term of the AP.
(ii) Find the sum of the first 12 terms of the AP.
(iii) Find which term of the AP is 91.
D) The following table shows the donation given by 50 students towards a Charitable trust.

| Donation in Rs <br> C.I | No of students <br> $f_{i}$ | Class marks <br> $x_{i}$ | $f_{i} x_{i}$ |
| :---: | :---: | :---: | :---: |
| $0-20$ | 5 |  |  |
| $20-40$ | 8 |  |  |
| $40-60$ | 10 |  | - |
| $60-80$ | 12 |  | - |
| $80-100$ | 7 |  | - |
| $100-120$ | 8 |  |  |
|  | $\sum f_{i}=50$ |  | $\sum f_{i} x_{i}=$ |

Rewrite and complete the table and find the mean donation by using the Direct Method.

Q2A) Attempt the following:
(i) If the sum and product of the roots of the quadratic equation are 5 and -6 respectively, then write the quadratic equation in $x$.
(ii) If one root of the quadratic equation $2 x^{2}+m x-15=0$ is -5 , then find the value of $m$.
B) Find the mode of the following frequency distribution table:

| Class Interval | Frequency |
| :---: | :---: |
| $20-30$ | 5 |
| $30-40$ | 12 |
| $40-50$ | 20 |
| $50-60$ | 8 |

C) Find the roots of the Quadratic Equation $5 x^{2}-14 x+8=0$ by using the "Factorisation Method."
D) Find the roots of the Quadratic Equation $3 x^{2}-4 x-7=0$ by using the "Quadratic Formula Method."

3A) Find the total surface area of a hemisphere of radius 7 cm .
( Do not substitute the value of $\pi$ )
B) Draw a line segment $A B$ of length 7.5 cm . Taking $A$ as centre and radius 3 cm , draw a circle. Using a pair of compasses and ruler, Construct tangents BP and BQ to the circle . Measure and state the length of the tangent segments.
C) Construct $\triangle \mathrm{PQR}$ with sides $\mathrm{PQ}=6.5 \mathrm{~cm}, \mathrm{QR}=7 \mathrm{~cm}$ and $\angle \mathrm{PQR}=60^{\circ}$. Using a pair of compasses and ruler, construct $\triangle P^{\prime} Q R^{\prime}$ similar to $\triangle$ PQR whose sides are $\frac{3}{4}$ of the corresponding sides of $\triangle$ PQR.
D) From the top ' $A$ ' of a tower ' $A B$ ' a man finds that the angle of depression of a car at point ' $C$ ' on the ground to be $30^{\circ}$. If the car is at a distance of 30 m from the foot of the tower, then find the height of the tower.
( Take $\sqrt{3}=1.73$ )


4A) Two identical solid cubes of side 2 cm are joined end to end. Find the volume of the resulting cuboid.
B) D and E are points on the sides AB and AC respectively of $\triangle A B C$, such that $\angle A D E=\angle A B C$. If $A D=1.5 \mathrm{~cm}, A B=6 \mathrm{~cm}, A E=3 \mathrm{~cm}$ and $D E=3.5 \mathrm{~cm}$, then
find i) $E C$
ii) $B C$

C) With reference to the given figure and the given conditions, write only the proof with reasons of the following theorem:


Given: In $\triangle$ DEF, $D E^{2}+E F^{2}=D F^{2}$
$\triangle P Q R$ is constructed such that $P Q=D E, Q R=E F$ and $\angle Q=90^{\circ}$
Prove that : $\triangle$ DEF is a right angled triangle.
D) Attempt the following :
(i) In the figure given below an open steel bucket is in the shape of a frustum of a right circular cone of height 15 cm . If the radii of its lower and upper ends are 12 cm and 20 cm respectively, then find
a) The slant height of the bucket
b) The curved surface area of the bucket ( Do not substitute the value of $\pi$ )

ii) A solid metallic cylinder of base diameter 6 cm and height 32 cm is melted to form 8 solid spheres of the same size.
Find the radius of each sphere.

